Pibretto

ASTROPHYSICAL RADIATION MAGNETOHYDRODYNAMICS

Being an Opera in Three Acts

PREMIERED

AT THE

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Words & Music By

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All the universe is a stage, And all matter and fields are merely players; They have their exits and entrances, And each, in their time, plays several parts.

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Now is the geometry of our discontent, Made gloriously invariant by this Sun of France; And all the aether that lowered upon our house, In the deep bosom of obscurity is buried.

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We at some times are minions of our theories, The fault, dear Brutus, is not in ourselves, But in our stars, that we are underlings. W I will not lend thee a quadrature! Why then the universe is my oyster---Which I with computer shall open, I will retort the knowledge in equipage. K

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